## Heuristic based approach for Novosibirsk traffic light scheduling

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## Introduction



## Simulation



## Simulation



## Solution representation



## Genetic algorithm

## Schema of genetic algorithm for minimization problem:

1. Chose an initial population $P=\left\{X_{1}, \ldots, X_{k}\right\}$ and keep a record value $f^{*}=\min f\left(X_{i}\right)$.
2. While stop criterion is not satisfied do the following:

- Chose two parents $X_{i_{1}}$ and $X_{i_{2}}$ from population.
- Apply a crossover operator to $X_{i_{1}}$ and $X_{i_{2}}$, obtain a new solution $X^{\prime}$.
- Apply a mutation operator to $X^{\prime}$, obtain a new solution $X^{\prime \prime}$.
- Doing a local descend from $X^{\prime \prime}$, obtain a new solution $X^{\prime \prime \prime}$.
- If $f\left(X^{\prime \prime \prime}\right)<f^{*}$, then update a record $f^{*}:=f\left(X^{\prime \prime \prime}\right)$.
- Add $X^{\prime \prime \prime}$ to population and delete the worst one.



## Objective functions

- Average time that the vehicles spent standing involuntarily (Waiting time)
- Average speed of the vehicles entered to simulation (average route length divided by average trip duration)

$$
\boldsymbol{F}=\frac{T T+S W+(N V * S T)}{V^{2}+P},
$$

TT - global trip time,
ST - simulation time,
SW - the time vehicles were obliged to stop and wait,
V and NV - the numbers of vehicles that reached and did not reach their destinations resp., P expresses proportion of colors in each phase j of all the intersections i: $P-\sum_{i} \sum_{j} s_{i j} \frac{G_{i j}}{\mathrm{C}_{i j}}$ with state duration $\mathrm{s}_{\mathrm{ij}}$, number $\mathrm{G}_{\mathrm{ij}}$ of traffic lights in green and $\mathrm{r}_{\mathrm{ij}}$ of traffic lignts in rea

* J.García-Nieto, E.Alba, A.Carolina Olivera. Swarm intelligence for traffic light scheduling: Application to real urban areas. Engineering Applications of Artificial Intelligence, 2012.


## Objective functions

Behavior of Waiting Time objective function


Rehavior of objertive function $\Gamma$


## Objective functions

Behavior of Average Speed objective function


| Objective function | Waiting Time | Av. Speed | F |
| :--- | :--- | :--- | :--- |
| Solution with the best Waiting Time | $\mathbf{6 3 . 1 4}$ | 5.87 | 14.40 |
| Solution with the best Av.Speed | 64.64 | $\mathbf{6 . 1 1}$ | 40.97 |
| Solution with the best value of F | 95.04 | 3.97 | 2.08 |

## Parameters of the algorithm

Initial population:

- Random vectors
- Local optima (random vectors + local descend)

Parents selection:

- The best individual in population with some other random one.
- Two parents chosen under geometric distribution with $p=0.3$ from the population sorted in ascending order of objective function value.

Crossover operator:

- One of parents coordinates
- Random number between two parents coordinates
- Mean value of parents coordinates


## Parameters of the algorithm

## Initial population

| Objective function | Waiting Time | Av. Speed | F |
| :--- | :--- | :--- | :--- |
| Initial population from random vectors | 66.47 | 5.97 | 2.33 |
| Initial population from local optima | 65.91 | 5.94 | 2.49 |

## Parents selection

| Objective function | Waiting Time | Av. Speed | F |
| :--- | :--- | :--- | :--- |
| Leader and random | 66.07 | 5.92 | 2.46 |
| Geometric distribution | 66.31 | 5.99 | 2.36 |

## Crossover operator

| Objective function | Waiting Time | Av. Speed | F |
| :--- | :--- | :--- | :--- |
| Random one | 64.63 | 5.98 | 2.34 |
| Random between | 66.53 | 5.89 | 2.51 |
| Mean value | 67.41 | 6.00 | 2.38 |

## Population degeneration

| Experiments set | Initial aver- <br> age distance | Average dis- <br> tance after <br> 15th itcration | Final average <br> distance |
| :--- | :--- | :--- | :--- |
| All | 1190.11 | 669.12 | 122.27 |
| Waiting Time obj.function | 1174.69 | 640.98 | 378.13 |
| Av.Speed obj.function | 1206.64 | 661.23 | 379.70 |
| Objective function F | 1189.90 | 705.16 | 508.98 |
| Init. popul. from local optima | 1186.20 | 714.14 | 522.63 |
| Random init. population | 1194.62 | 624.11 | 321.92 |
| Select leader and random | 1193.87 | 701.97 | 451.69 |
| Select under geom. distr. | 1186.94 | 636.28 | 392.85 |
| Crossover "random one" | 1196.81 | 756.51 | 494.33 |
| Crossover "random between" | 1192.78 | 619.30 | 379.71 |
| Crossover "mean" | 1181.64 | 631.56 | 392.77 |

## Final results

| Fitness | Vehicles | Schedule | Algorithm |
| :---: | :---: | :---: | :---: |
| 813 | 2462 | $[9,60,13,30,52,29,8,22,44,20]$ | GA+LS |
| 822 | 2448 | $[10,60,8,36,60,39,17,42,41,27]$ | GA+LS |
| 827 | 2443 | $[10,60,18,25,32,18,8,42,53,25]$ | GA+LS |
| 818 | 2450 | $[11,60,21,22,60,33,22,43,41,26]$ | GA |
| 819 | 2456 | $[8,60,24,20,55,49,8,32,46,32]$ | GA |
| 822 | 2459 | $[8,60,25,19,60,38,11,60,36,25]$ | GA |
| 1683 | 1822 | $[11,22,57,33,27,37,8,40,53,29]$ | initial |

## Thank you for attention!



## Any questions?

